

Name: _____
Pre-Calculus

Date: 12/1/14
Ms. Wilson

Unit 3: Exponential, Logistic, and Logarithmic Functions
Homework Packet #1 – Due 12/8/14

For questions 1-6, which of the following are exponential functions? For those that are exponential functions, state the initial value and the base. For those that are not, explain why not.

1.) $y = x^8$

2.) $y = 3^x$

3.) $y = 5^x$

4.) $y = 4^2$

5.) $y = x^{\sqrt{x}}$

6.) $y = x^{1.3}$

For questions 7-10, state whether the function is an exponential growth or exponential decay function. Sketch the function, and describe its end behavior using limits.

7.) $f(x) = 3^{-2x}$

8.) $f(x) = \left(\frac{1}{e}\right)^x$

9.) $f(x) = 0.5^x$

10.) $f(x) = 0.75^{-x}$

- 11.) The number B of bacteria in a petri dish culture after t hours is given by $B = 100e^{0.693t}$.
- a.) What was the initial number of bacteria present?
 - b.) How many bacteria are present after 6 hours?

- 12.) Using 20th century US census data, the population of New York state can be modeled by $P(t) = \frac{19.875}{1 + 57.993e^{-0.0353335t}}$, where P is the population in millions and t is the number of years since 1800.

Based on this model,

- a.) What was the population of New York in 1850?
- b.) What will New York state's population be in 2010?
- c.) What is New York's maximum sustainable population (limit to growth)?

For questions 13-20, determine the exponential function that satisfies the given conditions.

- 13.) Initial value = 5, increasing at a rate of 17% per year.

- 14.) Initial value = 52, increasing at a rate of 2.3% per day.

- 15.) Initial values = 16, decreasing at a rate of 50% per month.

16.) Initial value = 5, decreasing at a rate of 0.59% per week.

17.) Initial population = 28,900, decreasing at a rate of 2.6% per year.

18.) Initial population = 502,000, increasing at a rate of 1.7% per year.

19.) Initial height = 18 cm, growing at a rate of 5.2% per week.

20.) Initial mass = 15 g, decreasing at a rate of 4.6% per day.

21.) The 2000 population of Jacksonville, Florida was 736,000 and was increasing at the rate of 1.49% each year. At that rate, when will the population be 1 million?

22.) The 2000 population of Las Vegas, Nevada was 478,000 and is increasing at the rate of 6.28% each year. At that rate, when will the population be 1 million?

23.) The half-life of a certain radioactive substance is 14 days. There are 6.6g present initially.
a.) Express the amount of substance remaining as a function of time t .
b.) When will there be less than 1 g remaining?

24.) The number of students infected with the flu at Springfield High School after t days is modeled by the function $P(t) = \frac{800}{1+49e^{-0.2t}}$.

- a.) What was the initial number of infected students?
- b.) When will the number of infected students be 200?
- c.) The school will close when 300 of the 800-student body are infected. When will the school close?

25.) The population of deer after t years in Cedar State Park is modeled by the function $P(t) = \frac{1001}{1+90e^{-0.2t}}$.

- a.) What was the initial population of deer?
- b.) When will the number of deer be 600?
- c.) What is the maximum number of deer possible in the park?